

# Validating a Method for Estimating Specific Conductance in Mining Wastewater

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ASMR CONFERENCE 2016: RECLAIMING THE WEST

SPOKANE, WA

JUNE 8, 2016

# Outline

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- Regulatory Framework
- Review of Previous Work
- Current Work
  - Objectives
  - Procedure
  - Analysis and Results
  - Conclusions

# Regulatory Framework

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# Regulatory Framework

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EPA and Army Corps of Engineers issued interim memorandum in April 2010 related to Appalachian mining

- Not legally binding
- Framework for approval of all pending and future permits through CWA
- Effluent conductivity between 300-500  $\mu\text{S}/\text{cm}$

# Regulatory Framework

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Final Guidance was issued by EPA in July 2011

- Conductivity limit of 300-500  $\mu\text{S}/\text{cm}$  maintained
- Individual ions should be regulated when overall conductivity limit cannot be attained
- States are ultimately responsible for issuing permits and can choose whether or not to follow guidance

# Previous Work

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# Conductivity Modeling

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- Knowledge gap: How ions contribute to overall conductivity at low to medium concentrations
- Theoretical models have been developed for higher ionic strength waters (i.e. Industrial waste, brine waters)
- Empirical model was developed in 2011 by R. B. McCleskey

# McCleskey Model

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- Empirical model for contribution of cations and anions, trace metals, and ion pairs
- Constituents were included in this study based on their presence in natural waters
- WATEQ4F was used to determine speciated concentrations of each chemical at a given pH and temperature



# McCleskey Model

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Model may be used for the following conditions:

- Ionic strength: 0.0004-0.7 mol/kg
- Temperature: 0-95°C
- pH: 1-10
- Conductivity: 30-70,000  $\mu\text{S}/\text{cm}$

# McCleskey Model

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To find  $\lambda_i$ , the specific conductance of an ion at 25°C, need:

- $I$ , the Ionic Strength
- $\lambda^\circ(T)$ , specific conductance at a given temperature
- $A(T)$ , an empirical constant
- $B$ , a second empirical constant

Each ion has a unique  $\lambda_i$ ,  $\lambda^\circ(T)$ ,  $A(T)$ , and  $B$

# Ionic Strength

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$$I = 1/2 \sum m_i z_i^2$$

# McCleskey Model

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$\lambda^\circ(T)$  for  $K^+$

$$\lambda^\circ(T) = 0.00304 T^2 + 1.261 T + 40.70$$

$\lambda^\circ(T)$  for  $H^+$

$$\lambda^\circ(T) = -0.01414 T^2 + 5.355 T + 224.2$$

# McCleskey Model

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**A(T)** for  $K^+$

$$A(T) = 0.00535 T^2 + 0.9316 T + 22.59$$

**B** for  $K^+$

$$B = 1.5$$

<u>Ion</u>	<u><i>A</i></u>	<u><i>B</i></u>
$K^+$	$0.00535T^2 + 0.9316T + 22.59$	1.5
$Na^+$	$0.00027T^2 + 1.141T + 32.07$	1.7
$H^+$	$-0.00918T^2 + 1.842T + 39.23$	0.3
$Li^+$	$0.00412T^2 + 0.4632T + 13.71$	0.2

# McCleskey Model

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McCleskey's Empirical Specific Conductance Equation:

$$\lambda_i = \lambda^\circ(T) - \frac{A(T)I^{1/2}}{1 + BI^{1/2}}$$

# McCleskey Model

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Predicted SC for the entire solution:

$$\text{Predicted Specific Conductance} = \sum \lambda_i m_i$$

$m_i$  is the concentration of the  $i^{\text{th}}$  ion in solution

# McCleskey Model

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Results of model were excellent, with 98% of the  $R^2$  values for predicted vs measured conductivity above 0.92

Software used to find  $m_i$  was WATEQ4F



# Current Work

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# Objectives

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Goal: Determine if MINEQL+ is an acceptable speciation software to use with McCleskey's equations

Exploratory study to determine if MINEQL+ and WATEQ4F yield similar results for  $m_i$  values

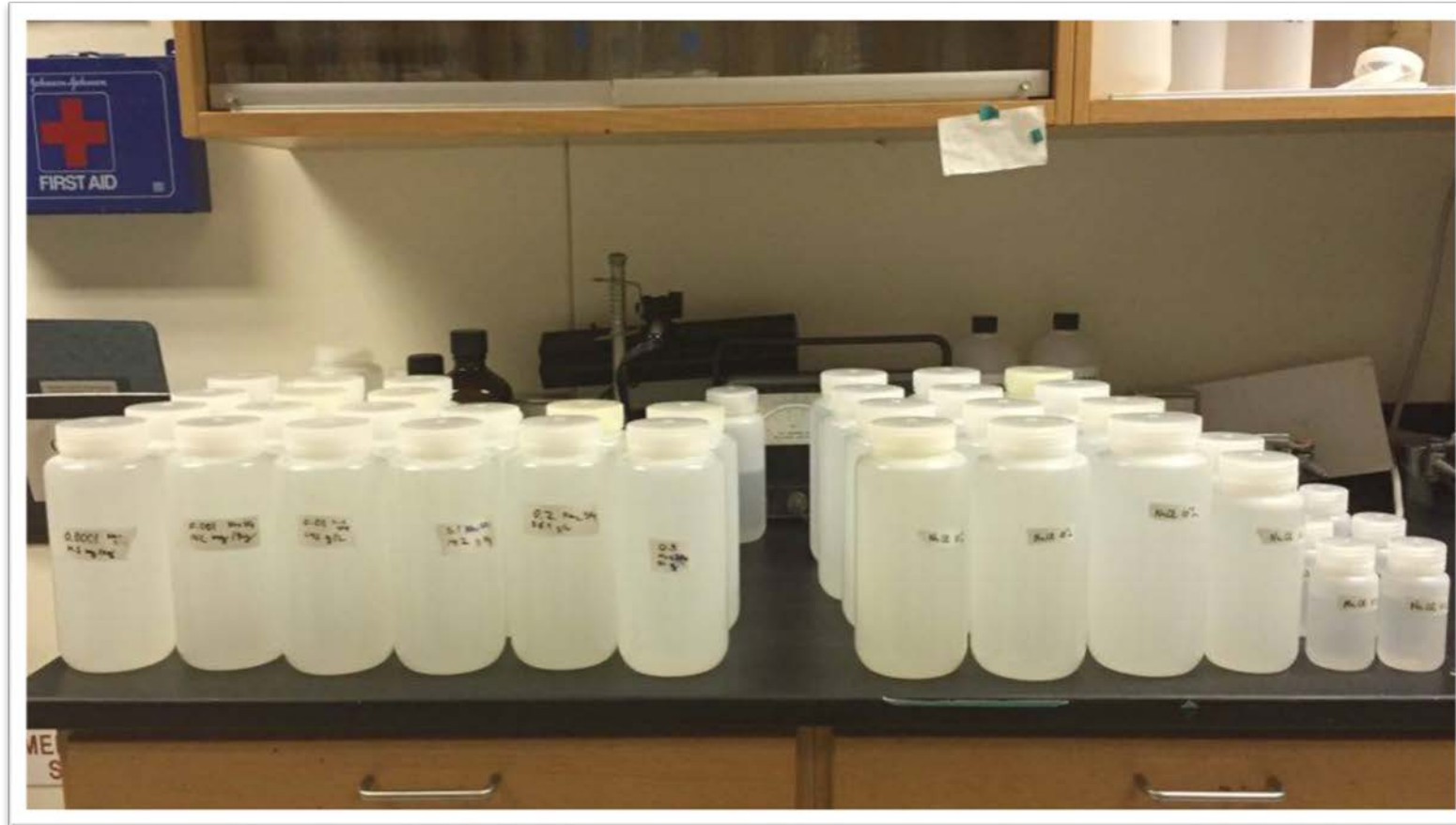
# Procedure

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- Solutions were created at six molalities (0.0001, 0.001, 0.01, 0.1, 0.2, and 0.5 m)
- Eight compounds were used ( $\text{NaHCO}_3$ ,  $\text{KNO}_3$ ,  $\text{MgSO}_4$ ,  $\text{K}_2\text{SO}_4$ ,  $\text{CaCl}_2 \cdot 2\text{H}_2\text{O}$ ,  $\text{Na}_2\text{SO}_4$ ,  $\text{KCl}$ , and  $\text{NaCl}$ )
- Temperature, pH, and SC were measured

# Procedure

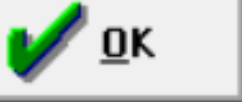

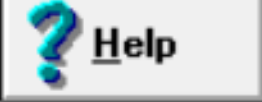
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# Procedure

- Determine species formed in solution

Calculation Wizard

Totals    pH    CO2

Component	Total C (M):
Cl(-)	1.00E-04
Na(+)	1.00E-04

Run: 1

ID	Species	Conc.
Type I - COMPONENTS		
2	H2O	1.000E+00
3	H(+)	4.900E-05
19	Cl(-)	1.000E-04
45	Na(+)	1.000E-04
Type II - COMPLEXES		
3800	OH- (-1)	1.640E-10
Type III - FIXED ENTITIES		
3801	H2O (Solution)	
175310	pH (+1)	

# Procedure

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-  $\lambda^0(T)$  and  $A(T)$ , and  $B$  determined for each species

Ion	$\lambda^0$	$A$	$B$
$K^+$	$0.003046T^2 + 1.261T + 40.70$	$0.00535T^2 + 0.9316T + 22.59$	1.5
$Na^+$	$0.003763T^2 + 0.8770T + 26.23$	$0.00027T^2 + 1.141T + 32.07$	1.7
$H^+$	$-0.01414T^2 + 5.355T + 224.2$	$-0.00918T^2 + 1.842T + 39.23$	0.3
$Li^+$	$0.002628T^2 + 0.7079T + 19.20$	$0.00412T^2 + 0.4632T + 13.71$	0.2

Source: McCleskey 2011

# Procedure

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Find the SC for each ion using McCleskey's equations

$$\lambda_i = \lambda^\circ(T) - \frac{A(T)I^{1/2}}{1 + BI^{1/2}}$$

# Procedure

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- For **each** concentration, find  $m_i$  for each ion in solution

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Run: 1
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ID	Species	Conc.
Type I - COMPONENTS		
2	H2O	1.000E+00
3	H(+)	4.900E-05
19	Cl(-)	1.000E-04
45	Na(+)	1.000E-04
Type II - COMPLEXES		
3800	OH-	(-1) 1.640E-10
Type III - FIXED ENTITIES		
3801	H2O (Solution)	
175310	pH	(+1)



# Procedure

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Find predicted SC for each concentration

$$\text{Predicted SC} = \sum \lambda_i m_i$$

# Procedure

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- Compared calculated and measured SC

<u>Sodium Chloride</u>			
	Measured	Predicted	
Goal (mol/kg)	SC (uS/cm)	SC (uS/cm)	% error
<b>0.0001</b>	12.8	28.3	121.0
<b>0.001</b>	123.3	123.3	0.0
<b>0.01</b>	1,180	1,112.5	5.7
<b>0.1</b>	10,220	9,826.8	3.8
<b>0.2</b>	19,140	18,608.0	2.8
<b>0.5</b>	44,100	42,856.7	2.8

# Results

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- 27% of values differed by more than 20%

	Compound							
Molality	Na <sub>2</sub> SO <sub>4</sub>	KNO <sub>3</sub>	CaCl <sub>2</sub>	MgSO <sub>4</sub>	NaHCO <sub>3</sub>	KCl	NaCl	K <sub>2</sub> SO <sub>4</sub>
<b>0.0001</b>	13%	88%	82%	64%	16%	42%	121%	2%
<b>0.001</b>	7%	9%	14%	1%	12%	8%	0%	2%
<b>0.01</b>	2%	7%	7%	29%	11%	8%	6%	0%
<b>0.1</b>	18%	2%	5%	60%	12%	4%	4%	5%
<b>0.2</b>	23%	1%	5%	59%	15%	5%	3%	6%
<b>0.5</b>	68%	12%	17%	65%	23%	4%	3%	42%

# Possible Explanations

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- Small mass of 0.0001 m solutions
- Ionic strength below suggested range
- Unknown problem with  $\text{MgSO}_4$
- Effect of temperature and pH
- Differences between  $\Delta H$  Values in MINEQL and WATEQ4F

$$\log\left(\frac{K_1}{K_2}\right) = \frac{-\Delta H^O}{R} \left(\frac{1}{T_2} - \frac{1}{T_1}\right)$$

# Low Concentration Solutions

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- Poor correlations for  $10^{-4}$  m solutions
- 0.0001 m solutions with  $> 20\%$  difference were remade
- Negative percent difference implies lower than stated chemical concentration

Original Solutions			
Compound	SC Measured	SC Calculated	% Difference
KNO <sub>3</sub>	13.8	25.9	-87.7%
CaCl <sub>2</sub>	19	34.5	-81.6%
MgSO <sub>4</sub>	14.7	24.1	-64.0%
KCl	15.9	22.6	-41.9%
NaCl	12.8	28.3	-121.0%

# Low Concentration Solutions

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- Chemicals adhere to measuring dish
  - Solution water poured over dish to ensure complete transfer

Compound	Original			Remade		
	SC Measured	SC Calculated	% Difference	SC Measured	SC Calculated	% Difference
KNO <sub>3</sub>	13.8	25.9	-87.7%	20.5	27.1	-32.2%
CaCl <sub>2</sub>	19	34.5	-81.6%	38.1	34.8	8.7%
MgSO <sub>4</sub>	14.7	24.1	-64.0%	28.5	24.4	14.4%
KCl	15.9	22.6	-41.9%	15.4	23.8	-54.5%
NaCl	12.8	28.3	-121.0%	14.9	28.6	-91.9%

# Low Concentration Solutions

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- Percent differences reduced but still fairly large
- Determined **low ionic strength** was the cause of errors
  - $I = 0.0001$ , lower threshold for use is  $0.0004$

Compound	Original			Remade		
	SC Measured	SC Calculated	% Difference	SC Measured	SC Calculated	% Difference
KNO <sub>3</sub>	13.8	25.9	-87.7%	20.5	27.1	-32.2%
CaCl <sub>2</sub>	19	34.5	-81.6%	38.1	34.8	8.7%
MgSO <sub>4</sub>	14.7	24.1	-64.0%	28.5	24.4	14.4%
KCl	15.9	22.6	-41.9%	15.4	23.8	-54.5%
NaCl	12.8	28.3	-121.0%	14.9	28.6	-91.9%

# Results

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- Half of remaining errors due to  $\text{MgSO}_4$

	Compound							
Molality	$\text{Na}_2\text{SO}_4$	$\text{KNO}_3$	$\text{CaCl}_2$	$\text{MgSO}_4$	$\text{NaHCO}_3$	KCl	NaCl	$\text{K}_2\text{SO}_4$
<b>0.0001</b>	13%	88%	82%	64%	16%	42%	121%	2%
<b>0.001</b>	7%	9%	14%	1%	12%	8%	0%	2%
<b>0.01</b>	2%	7%	7%	29%	11%	8%	6%	0%
<b>0.1</b>	18%	2%	5%	60%	12%	4%	4%	5%
<b>0.2</b>	23%	1%	5%	59%	15%	5%	3%	6%
<b>0.5</b>	68%	12%	17%	65%	23%	4%	3%	42%



# Magnesium Sulfate

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- Positive percent error
  - Solution has higher than predicted concentration

<b>Molality</b>	<b>SC Measured</b>	<b>SC Calculated</b>	<b>Percent Error</b>
<b>0.0001</b>	28.5	24.4	14.4
<b>0.001</b>	194.8	197.5	-1.4
<b>0.01</b>	1,463	1,045.5	28.5
<b>0.1</b>	8,940	3,599.7	59.7
<b>0.2</b>	15,300	6,307.1	58.8
<b>0.5</b>	30,500	10,570.8	65.3

# Magnesium Sulfate

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- High measured concentration is counterintuitive
  - Magnesium sulfate is hygroscopic
  - Pure  $\text{MgSO}_4$  mass typically less than measured chemical mass
- Corrective measures:
  - Confirm solution concentration using ICP
  - Measure conductivity and pH at 25°C
  - Replicates

# Sensitivity Analysis

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The effect of temperature and pH on predicted conductivity values was explored

- Greater understanding of effect on percent error values
- Potential for simplification of inputs to both MINEQL and empirical equations

# Sensitivity Analysis

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Changes explored:

- pH alone
- Temperature in MINEQL+ alone
- Temperature in empirical equations alone
- Temperature in both empirical equations and MINEQL+

# Sensitivity Analysis : Results

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- Changes to pH and temperature within MINEQL+ had minimal effect on predicted SC
- Temperature changes in empirical equations had much greater effect on predicted SC

$\lambda^0$	$A$
$0.003046T^2 + 1.261T + 40.70$	$0.00535T^2 + 0.9316T + 22.59$
$0.003763T^2 + 0.8770T + 26.23$	$0.00027T^2 + 1.141T + 32.07$

# Conclusions

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- Further work includes:
  - Replicates and expansion of tested compounds
  - Confirmation of chemicals in solution (ICP)
  - Comparing MINEQL+ and WATEQ4F for differences in constants and assumptions

# Conclusions

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- Sensitivity analysis
  - Changes in MINEQL+ affect predicted SC far less than changes to empirical equation temperature input
- Additional work needed before MINEQL+ may be used in place of WATEQ4F with McCleskey's equations

# Acknowledgements

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# Questions

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